

Rule ordering

Preprint version. Published in M. van Oostendorp, C. Ewen, B. Hume, K. Rice, eds., *The Blackwell Companion to Phonology*. Oxford: Wiley-Blackwell, 2011, 1736-1760.

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1. The bases of rule ordering

The distributional properties of sound in natural languages are explained by resorting to a level of underlying structure in addition to the level of observed phonetic or surface representation, and to a function that maps underlying representations into surface representations. This function was conceived since the beginning of generative grammar as a (partially) ordered set of rules. A rule expresses a significant generalization about the sound structure of a given natural language. The rules of Generative phonology, as formalized in Chomsky and Halle (1968) (henceforth SPE) and subsequent work, were formalized adaptations of descriptive statements about phonology of earlier frameworks, even though their function was not the same. Both the relationship of generative rules to statements of descriptive grammars and the reasons for imposing ordering on them can be gathered from the following example taken from Halle (1962: 57-58). (1a-d) correspond to the description of Sanskrit vowel sandhi in Whitney's *Sanskrit Grammar* (Whitney 1889). (1e-h) is a formalization of the corresponding generative rules. In (1e-h) I have included only the rules that apply to front vowels for simplification.

- (1) a. Two similar simple vowels, short or long, coalesce and form the corresponding long vowel. (§126)
- b. An *a*-vowel combines with a following *i*-vowel to *e*; with a *u*-vowel, to *o*. (§127)
- c. The *i*-vowels, the *u*-vowels and the *r* before a dissimilar vowel or a diphthong, are each converted into its own corresponding semi-vowel, *y* or *v* or *r*. (§129)
- d. Of a diphthong, the final *i*- or *u*-element is changed into its corresponding semi-vowel *y* or *v*-vowe before any vowel or diphthong: thus *e* (really *ai*...) becomes *ay*, and *o* (that is *au* ...) becomes *ay*. (§131)
- e. $V_i V_j \rightarrow V_i: \quad V_i = V_j$
- f. $ai \rightarrow e$
- g. $i \rightarrow j / _ V_i \quad V_i \neq i$
- h. $i \rightarrow j / V_i _ V_j \quad V_j \neq i$

The similarity of the rules to the descriptive statements is obvious. But, as Halle notices, if the ordering e-g-f shown by the arrows is imposed on the rules, "significant simplifications can be achieved." A similar comment is made in SPE (p. 18) with respect to ordering: "it [is] possible to formulate grammatical processes that would otherwise not be expressible with comparable generality." Indeed, the condition on dissimilarity of (1g) can be eliminated, since

when (1g) applies all similar VV sequences will have coalesced by the application of (1e). Moreover, (1h) can be dispensed with because ViV sequences will not be turned into eV by (1f) since (1g) will have changed the vowel into a glide.

Since SPE relates underlying and surface representations via a set of ordered rules, it follows that language variation must be due to differences in underlying representations, in the set of rules, and in their ordering. A famous example of difference in grammars stemming from different orderings of the same rules is Canadian raising, an example introduced in Halle (1962:63-64), based on data from Joos (1942), which is also discussed in Chomsky and Halle (1968: 342).

In certain Canadian and U.S. dialects the first elements in the diphthongs / $\text{e}\text{ɪ}$ /, / $\text{e}\text{ɪ}$ / are raised to $[\text{e}\text{ɪ}]$, $[\text{e}\text{ɪ}]$ before voiceless consonants.¹ At the same time there is regular voicing of / t / to $[\text{d}]$ or $[\text{ɾ}]$ in the American English flapping environment. The interaction of these phenomena gives different results in two dialects, A and B. This causes, according to Joos, a dilemma: in a word like *writer*, which is pronounced $[\text{w}\text{ɪ}\text{t}\text{ə}\text{r}]$ in dialect A, Joos's generalization that "/ a / is a lower-mid vowel ...[only] in diphthongs followed by fortis [\approx voiceless] consonants" is not true—and in Joos's view, descriptive statements are about surface representations, hence true of surface representations. Halle's solution to the dilemma stems from the recognition that statements of regularities ("rules") should be true of steps in the derivation, but need not be true of surface representations. This is the case if rules are ordered, and hence the application of a later rule can change the context that conditioned an earlier rule, as in this case, or the result of the rule itself. The statement in (2c=2b') is true of both surface representations (2d, d'), but the rule in (2b=2c') is true of (2d'), but not of (2d) which contains the sequence $[\text{e}\text{ɪ}\text{t}\text{ə}\text{r}]$, if we interpret the rule in the sense that "/ $\text{e}\text{ɪ}$ /, / $\text{e}\text{ɪ}$ / appear [phonetically] only before voiceless consonants." I simplify the flapping context to V_V .

(2) Dialect A

Dialect B

a.	/ $\text{e}\text{ɪ}\text{t}\text{ə}\text{r}$ /	a.'	/ $\text{e}\text{ɪ}\text{t}\text{ə}\text{r}$ /
b.	$\text{e}\text{ɪ} \rightarrow \text{e}\text{ɪ} / _ [C, -\text{voice}]$	$\text{e}\text{ɪ} \rightarrow \text{e}\text{ɪ} / V_V$	$\text{e}\text{ɪ} \rightarrow \text{e}\text{ɪ} / _ [C, -\text{voice}]$
c.	$\text{t} \rightarrow \text{d} / / V_V$	c.'	$\text{t} \rightarrow \text{d} / _ [C, -\text{voice}]$
d. Output:	$[\text{e}\text{ɪ}\text{t}\text{ə}\text{r}]$	d.'	Output:
	$[\text{e}\text{ɪ}\text{t}\text{ə}\text{r}]$		

Another example of grammars differing only in rule ordering is examined in Kiparsky (1982: 65-66). German devoices obstruents in coda position (3a) and simplifies tt clusters to t (3b). Two of the inflective forms of the adjective meaning 'long', *lang* and *lange* contrast in two

¹ I transcribe the diphthong vowel as $[\text{e}\text{ɪ}]$, and the voiced t as $[\text{d}]$, following Chambers (1973, 2006); Joos's phonetic description is slightly different (basically $[\text{e}\text{ɪ}]$ and $[\text{e}\text{ɪ}]$, respectively). Canadian raising has generated quite some discussion. Kaye (1990) casts some doubts on the existence of dialect B, that are not clearly motivated. Mielke et al. (2003) claim that the difference has been phonemicized, e.g. as $v/\text{e}\text{ɪ}\text{t}\text{ə}\text{r}/$ vs. $/\text{e}\text{ɪ}\text{t}\text{ə}\text{r}/$, but Idsardi (2006) argues convincingly that there are actual alternations.

dialect groups, one showing [□□□□], [□□□□], the other: [□□□], [□□□□], respectively. Application of any of the two rules renders the other rule inapplicable (mutual bleeding), therefore only the first rule applies in each ordering to underlying /□□□□/:

(3) a. Devoicing [obstr] → [-voiced] / ___ $\left. \begin{array}{l} [+C] \\ \{ \quad \} \end{array} \right\}$

b. g-deletion g → ∅ / [+nasal] ___

c. Dialect group I

	/□□□□/	/□□□□+□/
Devoicing	□□□□□□	□—□
g-deletion	—	□□□□

d. Dialect group II

	/□□□□/	/□□□□+□/
g-deletion	□□□□	□□□□
Devoicing	—	—

Rule ordering is closely connected to rule application. As witnessed by Whitney's example, descriptive grammars and many versions of structuralist phonology implicitly assume simultaneous rule application (see Postal 1968: 140-152). This follows from the assumption that rules (or descriptive statements) are true of surface representation—are generalizations about surface representation. In simultaneous rule application the string is scanned for the structural description of each rule and all the rules whose structural description is met apply simultaneously. Chomsky and Halle (1968: 19) provide an interesting abstract example of simultaneous application, which is compared to rule ordering.² I adapt it with a hypothetical example. Consider rules (4a), (4b), the underlying representations (4c) and (4d), and the results of simultaneous application (4e), and ordered rules (4f, g):

(4) a. □ → □□ /— □□
b. □ → □ /—□□□□□

□

□

Underlying

Surface

e□□ Simultaneous application f.□ Ord. a-b g. Ord. b-a

□	c.	/□□□/	□□□□□□	□□□□□	□□□□
□	d.	/□□□□/	t□□□□□	□□□□□	□□□□□

The problem is now empirical, i.e. the question to ask is whether natural languages have input-output relations like (4c,d-e), or rather input-output relations like (4c,d-f) or (4c,d-g). The latter are cases of mutually feeding rules. With the ordering (4a)-(4b) feeding takes place in /□□□□/ → □□□□□□ → [□□□□□□]; with the ordering (4b)-(4a) feeding takes place in /t□□□□□/ → □□□□□□ →

² Chomsky and Halle's (1968) example consists of the rules B → X / ___ Y and A → Y / ___ X and the input representations /ABY/, /BAX/.

[□□□□□]. Simultaneous application makes these feeding relationships impossible. Thus, since feeding relations are clearly observable in natural languages, rule ordering is supported, at least in front of simultaneous application.

A similar example can be constructed with mutually bleeding rules. Consider a language with palatalization of velars before *i* and backing of *i* to *u* after velars, and the underlying representation /□□/:

- (5) a. □ → □□ / __ □□
 b. □ → □ / k __ □□□
- □ Underlying Surface
- d. Simultaneous application e. Ord. a-b f. Ord. b-a
- c. □□□ □□□□□ □□□□ □□

Under rule ordering, for order (5a)-(5b) we can only apply palatalization (/□□/→□□□→—). For order (5b)-(5a) we can only apply backing (/□□/→□□→—). Here simultaneous application makes bleeding impossible: both rules must apply. Simultaneous application faces another problem. A set of ordered rules assigns one and only one surface representation to any underlying representation. But consider simultaneous application of two rules, one lowering mid nasalized vowels (e.g., □□ → □□), another raising mid unstressed vowels (e.g., □ → □, if unstressed). They will force / □□□□/ → [□□□□], / □□/ → [□□], under any application mode. But consider unstressed / □□□/, which satisfies both rules. Under ordering, the first rule applied always wins (we have again mutual bleeding): with the ordering lowering-raising the vowel is lowered, with the reverse ordering it is raised. Under simultaneous application, since / □□□/ meets the structural description of both rules, two simultaneous contradictory changes must apply to / □□□/: it has to be lowered *and* raised.

An ordering relation between rules A and B is often referred to as *extrinsic* ordering. On the other hand, *intrinsic* ordering refers to an ordering imposed by the form of the rules; when a rule is unordered with respect to another rule it can be the case that it is inapplicable unless the other rule has applied. This is typical of rewriting systems that generate an infinite set of representation from an initial symbol, as in phrase structure grammars like (6):

- (6) i. S → NP VP
 ii. NP → Det N
 iii. VP → V S

In (6) rule (6i) is intrinsically ordered before rule (6ii) and before rule (6iii) because their structural description cannot be met until (6i) has applied. In generative systems like (6) the ordering is generally free: different orderings generate different structures. Multiplicity of structures derived from the initial symbol (S in (5)) stem from unordering and from recursivity. On the contrary, in interpretive rule systems like classic generative phonology and other phonological theories an underlying representation is interpreted as a single surface representation (up to free variation).

Rule ordering was widely discussed in the 70's and beginning of the 80's, and a variety of different types of ordering were proposed. For details, see Iverson (1995) and especially Kenstowicz and Kisseberth (1977: 155-195).

2. Rule interaction, ordering, and applicability: feeding and bleeding

In a system of ordered rules, rules can interact: both the applicability and the result of application of a rule can depend on the application of previous rules. In 1968 Kiparsky introduced the notions of *feeding* and *bleeding* relations among rules in order to explain the direction of linguistic change. These concepts have been widely used afterwards. In this section I examine them in some detail.

Since it is not uncommon to detect some terminological inadequacies in the literature, in order to avoid confusion I will start with some terminological observations. In Kiparsky's original terminology, *feeding* and *bleeding relations* between rules are distinguished from *feeding order* and *bleeding order*. Feeding and bleeding relations (or the terms 'X feeds/bleeds Y') are defined as functional relations between two rules, with no actual ordering between them presupposed. *A feeds B* if *A* "creates representations to which *B* is applicable"; *A bleeds B* if *A* "removes representations to which *B* would otherwise be applicable.", where "representations" means *possible* representations (Kiparsky 1968: 37, 39). *Feeding order* and *bleeding order* are relations between rules that are in a specific order. Since feeding and bleeding relations are functional relations between rules, whether two rules are in feeding and bleeding relation can be determined by mere inspection of the rules.³ I will keep this distinction (feeding/bleeding relation vs. feeding/bleeding order), but I will reserve the use of the predicates *feed* and *bleed* applied to arguments *A* and *B* for feeding/bleeding order, and I will resort to the predicates *p-feed* and *p-bleed* ('p' for 'potentially') in the case of feeding/bleeding relations. (7) includes an illustration with our previous German example in (3):

(7)		German, group II (ord. g-del.-Dev.)
Feeding/bleeding relation	A p-feeds/p-bleeds B	g-deletion p-bleeds Devoicing Devoicing p-bleeds g-deletion
Feeding /bleeding order	A feeds/bleeds B	g-deletion bleeds Devoicing Devoicing does not bleed g-deletion

Feeding and bleeding relations can be formally defined as follows:

³ Of course one might want to relativize these notions to a given set of representations, e.g. the lexicon. For instance, a rule *A* that centralizes the place of articulation of all consonants in word final position feeds a rule *B* that vocalizes *l* to *w* in coda position, because it can create the representation ...*V*□]Coda### from . /...*V*□]Coda###/, to which *B* is applicable. But in a language with a single lateral *l*, the feeding interaction will never take place. In such cases we can say that *A* feeds *B*, but *A* doesn't feed *B* for lexicon *L*, or that *A* doesn't *L*-feed *B*. Similarly, if we relativize feeding and bleeding to specific derivations, we can say that a rule *A* does/does not *d*-feed or *d*-bleed a rule *B* meaning that the feeding or bleeding relation is not actually instantiated in that particular derivation.

(8) Feeding and bleeding relations

Rule A is in feeding relation wrt B (or A p-feeds B) iff there is a possible input I such that B cannot apply to I, A can apply to I, and B can apply to the result of applying A to I.

Rule A is in bleeding relation wrt B (or A p-bleeds B) iff there is a possible input I such that B can apply to I, A can apply to I, and B cannot apply to the result of applying A to I.

It is important to notice that in the definitions in (8) "apply" is usually interpreted as "apply non-vacuously". In the German example in (3), in dialect group I Devoicing bleeds g-deletion, (/p/ → /p̥/ → —). But for the word *Bank* 'bank' whose derivation is /p/ → (vacuous devoicing) p̥ → —, we don't want to say that devoicing bleeds g-deletion because the input to devoicing didn't meet already its structural description. Kiparsky's (1968) terms "creates" and "removes" above already indicate that vacuous application doesn't count.

On the other hand, *feeding order* and *bleeding order* (or the terms *A feeds B* and *A bleeds B*) refer to relations between two rules A and B that presuppose both feeding/bleeding and the specific ordering A < B in the grammar. Most definitions are formulated for cases in which A immediately precedes B, or cases in which intervening rules don't interact with A and B. In such a situation the definitions become simpler: A is in feeding/bleeding order wrt B iff A < B (i.e., A precedes B) and A feeds/bleeds B. For the general case the definitions have to be refined as follows:

(9) Feeding order and bleeding order

Let G be a grammar, A, B rules, and D a derivation of G.

a. A is in *feeding order* wrt B (or A *feeds* B) in grammar G iff

i) A < B

ii) There is a derivation D by G such that B would not apply to the input to A, and B applies to the output of A and would apply to all intermediate stages up to its own input.

b. A is in *bleeding order* wrt B (or A *bleeds* B) in grammar G iff

i) A < B

ii) There is a derivation D by G such that B would apply to the input to A, and B does not apply to the output of A and would not apply to all intermediate stages up to its own input.

When A immediately precedes B or in cases where intermediate rules don't interact we get derivations like those in (10): (10ai) is in feeding order wrt to (10aai) because the second rule (10aai) wouldn't apply to AQ but it applies to BQ, the output of the first rule (10ai); (10bi) is in bleeding order wrt to (10bii) because the second rule (10bii) would apply to AQ but it doesn't apply to BQ, the output of the first rule (10bi).

(10) (No intervening interacting rules)

a. Feeding order

- | | |
|------------------------------|----|
| | AQ |
| i. $A \rightarrow B / _ Q$ | BQ |
| ii. $Q \rightarrow R / B _$ | BR |

b. Bleeding order

- | | |
|------------------------------|----|
| | AQ |
| i. $A \rightarrow B / _ Q$ | BQ |
| ii. $Q \rightarrow R / A _$ | — |

Feeding order (a rule A feeds a rule B) can be illustrated with the interaction of $\text{[y]} \rightarrow \text{[ø]}$ and Umlaut in a group of Swiss German dialects (Kiparsky 1982: 190), bleeding order (rule A bleeds rule B) with our earlier example (2a'-d'), Canadian raising in the word *writer* for dialect A:

(11) Feeding. Swiss German, Group I / $\text{[y]} \rightarrow \text{[ø]}$ -li/ 'egg-diminutive'

- | | |
|---|---|
| A. $\text{[y]} \rightarrow \text{[ø]} / _ C, \#\#$ | $\text{[y]} \rightarrow \text{[ø]}$ |
| B. Umlaut (fronting) | $\text{[y]} \rightarrow \text{[ø]}$ (B. would not apply nonvacuously to / $\text{[y]} \rightarrow \text{[ø]}$ -li/) |

Bleeding. Canadian raising, dialect A

- | | |
|--|---|
| A. $\text{[y]} \rightarrow \text{[ø]} / V _ V$ | $\text{[y]} \rightarrow \text{[ø]}$ |
| B. $\text{[y]} \rightarrow \text{[ø]} / _ [C, \text{-voice}]$ | — (B. would apply to / $\text{[y]} \rightarrow \text{[ø]}$ /) |

Consider now the cases with interacting rules intervening between A and B that motivate the definitions in (9). (12a) exemplifies feeding and (12b) bleeding cases. A and B are the rules in feeding/bleeding relation, C is the intervening rule.

(12) (Intervening interacting rules)

a. (Non-)feeding order

- | | |
|-----------------------------|----|
| | QA |
| A. $Q \rightarrow R / _ A$ | RA |
| C. $A \rightarrow B / R _$ | RB |
| B. $A \rightarrow C / R _$ | — |

b. (Non-)bleeding order

- | | |
|-----------------------------|----|
| | QA |
| A. $Q \rightarrow R / _ A$ | RA |
| C. $A \rightarrow B / R _$ | QA |
| B. $A \rightarrow B / Q _$ | QB |

In the feeding example, rule A p-feeds rule B and preceds B, but given conditions (9aii, bii), it does not feed rule B, because some rule ordered between them, namely C, undoes the change that caused the feeding (it bleeds rule B). In terms of the definitions in (9), there are representations between the two rules, in particular the input to rule B, to which the second rule cannot apply. Similarly, in the bleeding example, rule A p-bleeds rule B and would indeed bleed rule B if it were not for C which feeds rule B.

Of course a pair of rules can show non-feeding or non-bleeding interactions like those in (12) in some derivations, but feeding or bleeding interactions in other derivations. I will use the terms d-feed and d-bleed when feeding and bleeding is relativized to a specific derivation. English stress provides an actual example for bleeding. Stress is assigned twice in words like *context* $[\text{ˈkɒntɛks}t]$ or *Ahab* $[\text{ə}ˈhɑːb]$. But after a light syllable the second stress is removed (Arab rule, Ross 1972), as in *Arab* $[\text{ə}ˈrɑːb]$, and the destressed vowel reduces to $[\text{ə}]$.

Stress bleeds vowel reduction, but in the derivation of *Arab* destressing undoes the bleeding (/□□□□/ → □□□□□□ → □□□□□□ → □□□□□□□□). Here we must say that stress bleeds reduction, because there are derivations that show actual bleeding, as in □□□□□□□, but if we relativize bleeding to specific derivations, some of them do not show a bleeding interaction: in these derivations stress doesn't d-bleed reduction.⁴

There is yet another interesting case of p-feeding/bleeding with no actual feeding/bleeding. If a rule A p-feeds a rule B and precedes it, and there is a representation to which A applies and B would not apply, it is possible according to (9), to have no feeding order even if, contrary to what happens in the previous examples, B actually applies. The same is true, mutatis mutandis, of bleeding order. This happens in Duke of York derivations, which are derivations in which a rule reverses the action of a previous rule, e.g. ...A... → ...B... → ...A... Consider the derivations in (13), which contain a Duke of York (sub)derivation, highlighted in bold (notice that (12b) above is also an instance of Duke of York):

(13) (Intervening interacting rules, Duke of York derivatons)

a. Feeding order

	QA
A. Q → R / __A	RA
C. A → B / R__	RB
D. B → A / R__	RA
B. A → C / R__	BC

b. Bleeding order

	QA
A. Q → R / __A	RA
C. A → B / R__	QA
D. A → B / Q__	QB
B. A → C / Q__	—

In (13a) A p-feeds and precedes B, and B does apply, but A does not feed B, because there is an intermediate representation to which the second rule would not apply, namely RB, created by C. In fact it is the other intervening rule, D, that now feeds A. Similarly, in (13b) A p-bleeds the last rule B, but it does not bleed it, even if the rule does not apply, because of the intermediate representation QA created by C, to which the rule would apply. Here it is rule D which actually bleeds B.

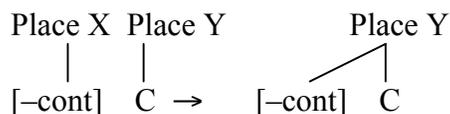
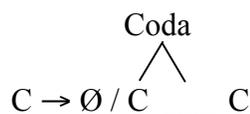
Feeding and bleeding interactions have been used in different contexts and for different purposes, so it is conceivable to have slightly different changes in the definitions. One such change is desirable in cases in which usual definitions do not yield a feeding/bleeding relation, and yet this relation is intuitively correct. Consider a case like (14) in which Glide Formation, Vowel Reduction, and Destressing interact in Central Catalan. (14a, b, c) show that Glide Formation affects postvocalic high unstressed vowels, but not nonhigh or stressed vowels. It also affects high unstressed vowels that are not underlying, as in (14d).

⁴ Notice that the example is adequate only if we assume that the underlying /□□□□/ has no stress structure and the unstressed character of the second vowel is introduced by the stress rule.

(14)	a.	b.	c.	d.
	ser[$\square\square$] [\square]mid	ser[$\square\square$] [\square]sirís	ser[$\square\square$] [$\square\square$]til	ser[$\square\square$]
	[$\square\square$]ciós			
	'it-will-be wet'	'it-will-be Osiris'	'it-will-be useful'	'it-will-be idel'
Destressing				$\square\square$ \square
Vowel Reduction				$\square\square$ \square
Glide Formation	$\square\square$ \square			$\square\square$ \square
Output:	ser[$\square\square$] [\square]mid	ser[$\square\square$] [\square]sirís	ser[$\square\square$] [$\square\square$]til	ser[$\square\square$] [\square]ciós

Notice now that the structural description $V V[+\text{high}, -\text{stress}]$ is met in (d) because Vowel Reduction has turned [\square] into a high vowel, but also because Destressing has created the other condition for gliding. In such case we want to say that these two rules jointly feed Glide Formation. The definitions in (9) can be accordingly changed to meet such situations. Consider yet another case, where the ordering is bleeding. A representation CAD is subject to two rules $C \rightarrow Q / _A$, $D \rightarrow R / A_$, that are unordered with respect to each other and which precede the rule $A \rightarrow B / C_D$. Each rule individually cannot change the representation CAD in such a way as to render the third rule inapplicable, but together they do. Since they are (mutually) unordered, the only way to establish a bleeding order is to say that they jointly bleed the third rule.

Notice also that a rule can both feed and bleed another rule, and stand in both feeding and bleeding order with respect to it. In Balearic Catalan stops assimilate in place to a following consonant (Place Assimilation), and the second consonant in a two-consonant coda cluster deletes before another consonant (Cluster Simplification). As shown in (15), deletion of the medial C causes bleeding when the medial C is the target of assimilation and feeding when it intervenes between the trigger and the target of assimilation.

(15) *Place Assimilation**Cluster Simplification*

		<i>Bleeding</i>	<i>Feeding</i>		
Input		$\square\square\square\square\square\square\square\square\square\square$	$\square\square\square\square\square\square\square\square\square\square$	'I	empty
'trains'		'empty trains'			
Cluster simplification		$\square\square\square\square\square\square\square\square\square\square$	$\square\square\square\square\square\square\square\square\square\square$		
Place Assimilation		— \square	$\square\square\square\square\square\square\square\square\square\square$		
\square Output:		$\square\square\square\square\square\square\square\square\square\square$	$\square\square\square\square\square\square\square\square\square\square$		

It is obvious that two rules cannot mutually d-feed each other in the same locus L: in the ordering $A < B$, if A feeds B, A must apply to L, and B must not be applicable; in the ordering $B < A$, B must apply to L, contradicting the first condition. But rules might mutually d-feed or

"Counter" orderings have important properties. Assume the simple case where rules A and B are adjacent, and $A < B$. Since in feeding order there must be at least one input I such that A is applicable to I, B is not, and B is applicable to the output of A (9), it follows that in the corresponding counterfeeding order where $B < A$ there must be an input (namely I) to which the first rule, now B, does not apply and to which the second rule, now A, applies. Hence the generalization expressed by B does not appear in the output: we can say, using McCarthy's (1999) terms that it is *not surface-true*, it is not true of the of the output of A, usually the surface representation. In bleeding order there must be by definition at least one input I such that both A and B are applicable to I, and B is not applicable to the output of A; it follows that in the corresponding counterfeeding order with $B < A$ there can be an input to which the first rule, now B, applies and to which the second rule, now A, does not apply. Hence the generalization expressed by A about the input I does not appear in the output: following McCarthy we can say that it is *not surface-apparent*, because the generalization A about I is not apparent in the output o A, usually the surface representation.

(19)	Feeding	Counterfeeding	Bleeding	Counterbleeding
	I	I	I	I
	B I'	B —	B I'	B I'
	A I''	A I'	A —	A —, I''

It is important to notice that the existential quantification in the definitions in (9) of feeding and bleeding orders (hence also of counterfeeding and counterbleeding orders) allows for the existence of multiple feeding and bleeding relations between two rules. For feeding, and given two ordered rules $A < B$, the requirement (9a_{ii}) that there be an input I whose derivation D meets the conditions required in (9a_{ii}) does not prevent the existence of another input I' that meets the condition (9b_{ii}) for bleeding. Hence A can both feed and bleed B (and B can both counterfeed and conterbleed A). Similarly, when we consider opposite orderings it can be the case that A feeds B and B feeds A (mutual feeding), and that A bleeds B and B bleeds A (mutual bleeding), or that A feeds B and B bleeds A. The remaining logical possibilities are that a rule feeds or bleeds another rule but doesn't bleed or feed it, respectively, and that there is no interaction in the opposite order.

The only restrictions in these cases of multiple interaction regards orders relative to a given single representation R. Obviously, a rule A cannot both feed and bleed a rule B for the same input I in the same locus of application. Less obviously, if A feeds B in the derivation of I, then B cannot feed or bleed A in the corresponding derivation of I. The only possibility is that A bleeds B and B bleeds A. The reason, for the first case, is that if A feeds B in the derivation of I, by definition B is not applicable to I, and if at the same time B feeds or bleeds A, then also by definition B should be applicable to I—hence a contradiction. But mutual S-bleeding is possible, as witnessedd by our German example in (3): Devoicing bleeds g-deletion for input $I = / \text{ } / (/ \text{ } / \rightarrow / \text{ } / \rightarrow \text{ })$, and g-deletion bleeds Devoicing in the same input $I = / \text{ } / (/ \text{ } / \rightarrow / \text{ } / \rightarrow \text{ })$.

Applicability of rules is also related to disjunctive ordering and to the Elsewhere Condition. SPE distinguishes between conjunctive ordering of two rules (the normal mode of application) and disjunctive ordering, where only one of the rules can apply. In SPE conjunctive ordering and disjunctive ordering derive from abbreviatory devices: ...{A B}... corresponds to two conjunctively ordered rules, ...A... and ... B..., ...A(B)... corresponds to two

apply to [nightingale] (*[nɪŋhtingale]) because it is underived. Again the identity rule [sɪn] ↔ [sɪn] cannot block TSS because the structural description of the identity rule [sɪn] and the structural description of shortening, [V C₀ V]_{StrF}, are not in proper inclusion relation, but in intersection. But [nightingale] properly includes [V C₀ V]_{StrF}. Cyclic effects in Iter cycles/levels derive from the assumption that the output of every cycle/level is a lexical item, hence an identity rule.

Given OT, some properties of Elsewhere-type interactions follow as a theorem, Panini's Theorem on Constraint-ranking (PTC) (Prince and Smolensky 1993/2004: §5.3, 7.2.1). PTC relates the activity of two constraints, S and G, in a constraint hierarchy relative to an input *i*. Assume that S applies nonvacuously to *i* (i.e., it distinguishes the set of candidates Gen(*i*)). If G ≫ S and G is active on *i* (i.e., it distinguishes the set of candidates Gen(*i*) when it applies) then S is not active on *i*.⁵

3. Serial and parallel approaches

Rule interactions of the sort just discussed have become important in the theoretical comparative analysis of serial and parallel approaches, in particular in relation to opacity [cross-reference to EB's chapter]. If we compare a standard serial theory like SPE and OT, pure feeding and pure bleeding order effects (i.e., those that are not also counterfeeding or counterbleeding) can be derived from both. Consider the well-known case of interaction of e-raising and t→s in Finnish (Kiparsky 1973: 166-172):

- (23)
- | | | | | |
|----|--------------|-----------------|---------|----------|
| | □□□□ | 'water-nom.sg.' | □□□□□-□ | 'wanted' |
| a. | e → i / __## | □□□□ | — | |
| b. | t → s / __i | □□□□ | □□□□□-□ | |

Because both (23a) and (23b) are statements that are true of surface forms, constraints of the form *e##, *□□, dominating conflicting faithfulness constraints, together with other constraints determining the choice of /□□□□□/, will derive the output of /□□□□□/, /□□□□□-□/. But consider now the example of mutually feeding rules in (4). Since they are mutually feeding they are also counterfeeding in both orderings:

- (24)
- | | | | | |
|----|---------------|---------|--------|---------------------|
| | | /□□□/□□ | /□□□□/ | |
| a. | □ → □□ / — □□ | c. | □□□□□□ | □— |
| b. | □ → □ /—□□□□ | d. | □□□□□□ | □□□□□ □□, not □□□□! |

In order to derive □□□□ from□□□□□□□□□□*□□□□ must dominate FAITH *e*, and *□□□ must dominate FAITH *t* (25a). But this ordering makes □□□□ from□□□□□□□□□□ impossible to obtain, because high-ranked *□□□ will force the victory of □□□□□□□□ as shown in (25b).

⁵ For a clear and interesting discussion of the relation between the Elsewhere Condition and PTC, see Bakovic (2006); see also Prince (1995).

(25) a.

/tʰtʰ/	*tʰtʰ	*tʰ	FAITH e	FAITH t
tʰtʰ		*		
☞ tʰ tʰtʰ			*	
tʰtʰ	*		*	*

b.

/tʰtʰtʰ/	*tʰtʰ	*tʰ	FAITH e	FAITH t
tʰtʰtʰ	*			
√ tʰ tʰtʰtʰ		*	*	
☞ tʰ tʰtʰtʰ			*	*

Therefore in counterfeeding ordering the first rule is not "surface true": its structural description $tʰtʰ$ appears in the phonetic representation without the corresponding structural change ($tʰ \rightarrow tʰtʰ$), because the second rule has introduced changes that would allow the application of the first rule. When the ordering is counterbleeding, the generalization expressed by the first rule is not "surface apparent" In Canadian raising, dialect A, the change $tʰtʰt \rightarrow tʰtʰt$ does not appear as such in the phonetic representation of *writer* because the second rule has changed the result of the change, turning the triggering voiceless $tʰ$ into t :

- (26) a. /tʰtʰtʰtʰ/ /tʰtʰtʰtʰtʰ/
- b. $tʰtʰtʰ \rightarrow tʰtʰtʰ / _ [C, -voice]$ tʰtʰtʰtʰ tʰtʰtʰtʰtʰ/
- c. $tʰ \rightarrow t / / V _ V$ tʰtʰtʰtʰ tʰtʰtʰtʰtʰ tʰtʰ, not tʰtʰtʰ!

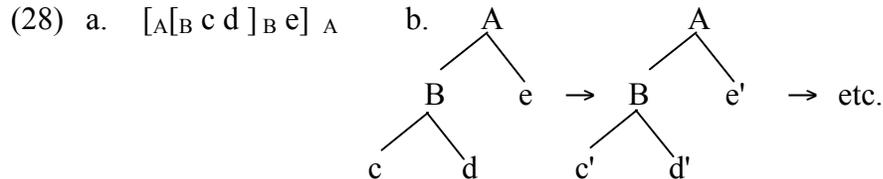
Here in order to obtain $tʰtʰtʰ$ in *type*, both $*tʰtʰ[C, -voice]$ and $*VtʰV$ must be active. But for *writer* the input /tʰtʰtʰtʰtʰ/ where both constraints are relevant cannot have as output $tʰtʰtʰtʰtʰ$ because the candidate $tʰtʰtʰtʰtʰ$ also satisfies both markedness constraints and is, in addition, more faithful to the input:

(27)

/tʰtʰtʰtʰtʰ/	*tʰtʰtʰ[C, -voice]	*VtʰV	FAITH tʰtʰ	FAITH t
tʰtʰtʰtʰtʰ	*	*		
√ tʰ tʰtʰtʰtʰ		*	*	
☞ tʰ tʰtʰtʰtʰ				*
tʰtʰtʰtʰtʰ			*	*

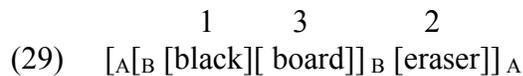
4. Cyclic ordering

In cyclic application the input to the set of rules is a phonological representation organized by constituent structure, which is represented in (28a) by (proper) bracketing, and by a tree in (28b); A, B are categories, and d, e, c are phonological strings, matrices, or structures.



The set of (partially) ordered rules \mathfrak{R} applies first separately to the innermost constituents, i.e. to c, to d, and to e, giving as a result c', d', e'. This is the first cycle. We now proceed to the second cycle, the next degree of embedding, namely B, and apply the set of rules to its domain, the concatenation c'□□□□d', whose output is (c'□□□□d')'. The domain of the following (and in this case the final) cycle is whatever is dominated by A, namely (c' □□ d')' □ e.

The cycle was first proposed in phonology (Chomsky, Halle, and Lukoff 1956) to deal with stress in compounds like *black board eraser* showing primary-tertiary-secondary stress distinctions:



After stress has applied to individual words, the compound stress rule locates stressed vowels and maintains primary stress on the leftmost stressed vowel and weakens other stresses by one degree. After assigning vacuously primary stress 1 in the first cycle to [bla₁ck], to [boa₁rd], and to [era₁ser], it applies in the second cycle in the domain B to [bla₁ck boa₁rd], yielding [bla₁ck boa₂rd], and in the last cycle in the domain A to [bla₁ck boa₂rd era₁ser] to give the final [bla₁ck boa₃rd era₂ser].

Cyclicity was later applied in syntax as a result of the elimination of generalized transformations and the generation of embedded sentences by base rules (Chomsky 1965). Later on, Chomsky (1973) proposed a limitation on cyclic application in syntax, the Strict Cycle Condition (SCC, or "strict cyclicity") by which no rule can apply to a constituent I in such a way as to affect solely a subconstituent of I. Kean (1974) presented two cases that argued for the application of the SCC also in phonology. In (28), for instance, in the second cycle, cycle B, a rule cannot apply to the domain of B if it just affects c'. An actual example is the interaction of Glide Formation and Destressing in Catalan. Glide Formation applies to postvocalic high vowels. In *produirà* 'it will produce' it cannot apply to [₂[₁□□□□□□□□]□□□□] at cycle 1 because postvocalic □□ is stressed. In cycle 2 a following stress causes destressing of □□. Therefore at cycle 3, and at later cycles, the sequence □□□□ meets the structural description of □□□□.

the rule; but $\square\square$ is entirely within cycle 1 and the SCC blocks application, resulting in $[\square\square\square\square\square\square\square\square], *[\square\square\square\square\square\square\square\square]$.

The SCC was further refined in Mascaró (1976:1-3) as in (27). Case (30Ba) corresponds roughly to the SCC as formulated in Chomsky (1973) and used by Kean (1974).

- (30) Given a bracketed expression $[_n \dots [_{n-1} \dots, [_{1\dots}]_1, \dots]_n \dots]_n$, and a (partially ordered) set of cyclic rules C,
- A. C applies to the domain $[_j \dots]_j$ after having applied to the domain $[_{j-1} \dots]_{j-1}$, each rule in C applying in the given order whenever it applies properly in j.
- B. *Proper application of rules.* For a cyclic rule R to apply properly in any given cycle j, it must make specific use of information proper to (i.e. introduced by virtue of) cycle j. [This situation obtains] if either a, or b or c is met:
- a. R makes specific use of information uniquely in cycle j. That is, it refers specifically to some A in $[_j XAY [_{j-1} \dots]Z]$ or $[_j Z [_{j-1} \dots] XAY]$.
- b. R makes specific use of information within different constituents of the previous which cannot be referred to simultaneously until cycle j. R refers thus to some A, B in $[_j X [_{j-1} \dots A \dots] Y [_{j-1} \dots B \dots] Z]$.
- c. R makes use of information assigned on cycle j by a rule applying before R.

A states the general procedure for cyclic application; B gives the conditions for proper application: morphologically derived environments in inflection (30Ba), derived environment by compounding or syntax (30Bb), and rule derived environments (30Bc). Effects of derived environments on application of processes, irrespectively of the theoretical mechanism they derive from, are usually referred to as *derived environment effects* (DEE). We just saw a case under (30Ba). The rule of $t \rightarrow s$ assibilation in Finnish illustrates both (30Ba) and (30Bc). Assibilation applies in morphologically derived environments (31c): the structural description $\square\square$ is met by material in the root cycle and in the inflected word cycle. It also applies in rule-derived environments (31d): here the structural description $\square\square$ is met because at its cycle of application a rule has created it. But it fails to apply in the nondervided environments (31e), because none of the conditions for proper application in (31B) is met:

- (31) a. $t \rightarrow s / _ _ i$
 b. $e \rightarrow i / _ _ \#\#$
- | | | | | |
|----|----------|--------------------|--|-----------------|
| c. | halut-a | 'to want' | halus-i | 'wanted' |
| | | | turpot-i | 'swelled' |
| | | | hakkat-i | 'hewed' |
| d. | vete-nä | 'water-essive.sg.' | vesi (\leftarrow veti \leftarrow vete) | 'water-nom.sg.' |
| | käte -nä | 'hand-essive.sg.' | käsi (\leftarrow vkäte \leftarrow käte) | 'hand-nom.sg.' |
| e. | tila | 'place, room' | | |

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